

**HAND ARM  
VIBRATION**



# Vibration emission of grinders: experiments and model

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Quentin PIERRON<sup>1</sup>

<sup>1</sup> Institut National de Recherche et de Sécurité pour la Prévention des Accidents du Travail et des Maladies Professionnelles (INRS)

[quentin.pierron@inrs.fr](mailto:quentin.pierron@inrs.fr)



# Summary

1. Introduction
2. First experimental tests: according to the standard EN 60745-2-3
3. Second experimental tests: hanged grinder
4. Numerical Model
5. Discussion



# Introduction

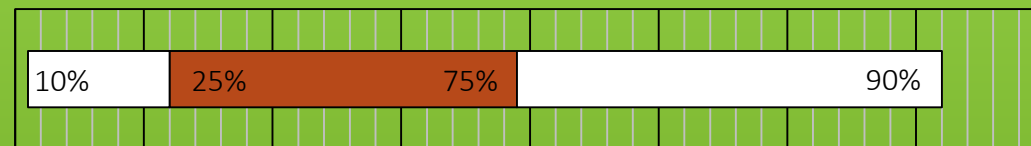


## Statistical total vibration exposure for angle grinders

**Vibration magnitude  $a_{hv}$  (m/s<sup>2</sup>)**

(frequency-weighted root-mean-square acceleration)

3 4 5 6 7 8 9 10 11



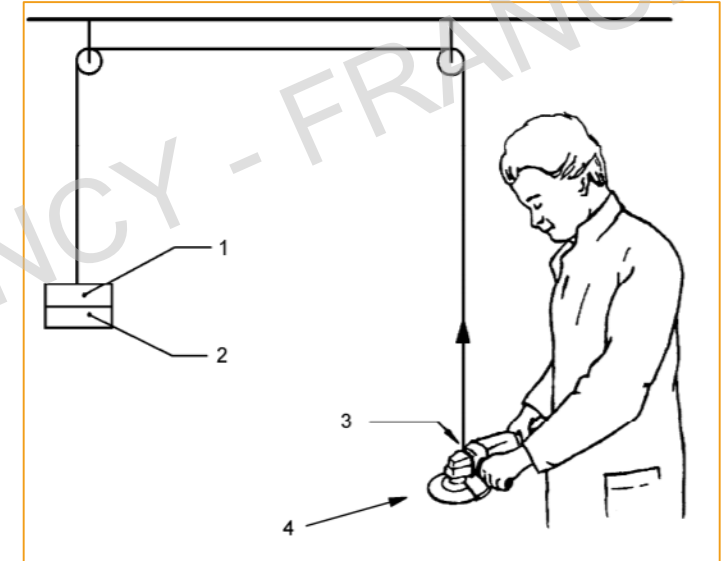
Data from  
*CEN/TR1030-2:2016*  
(106 measurements  
between 2005-2014)

# Introduction

Real condition



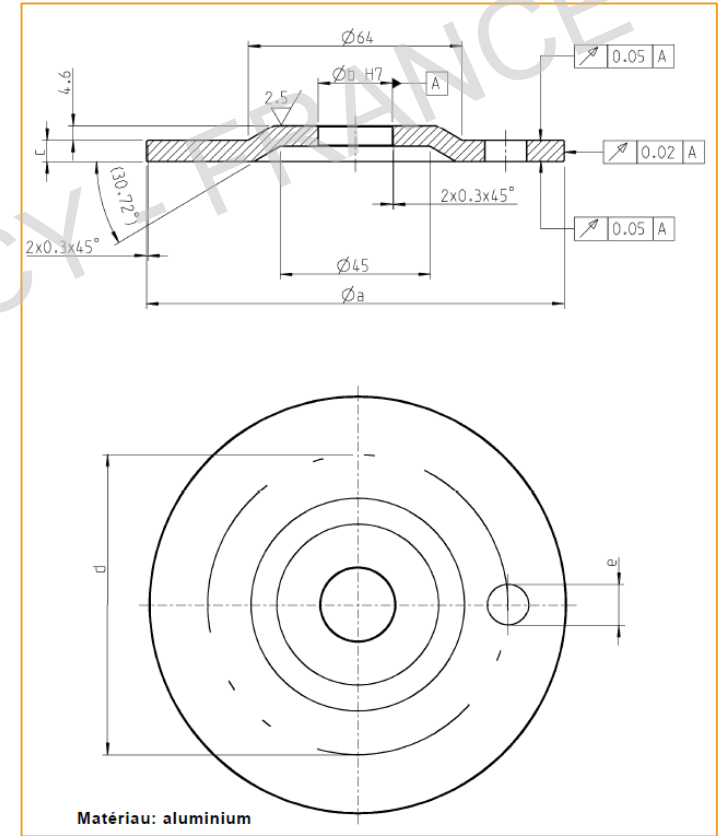
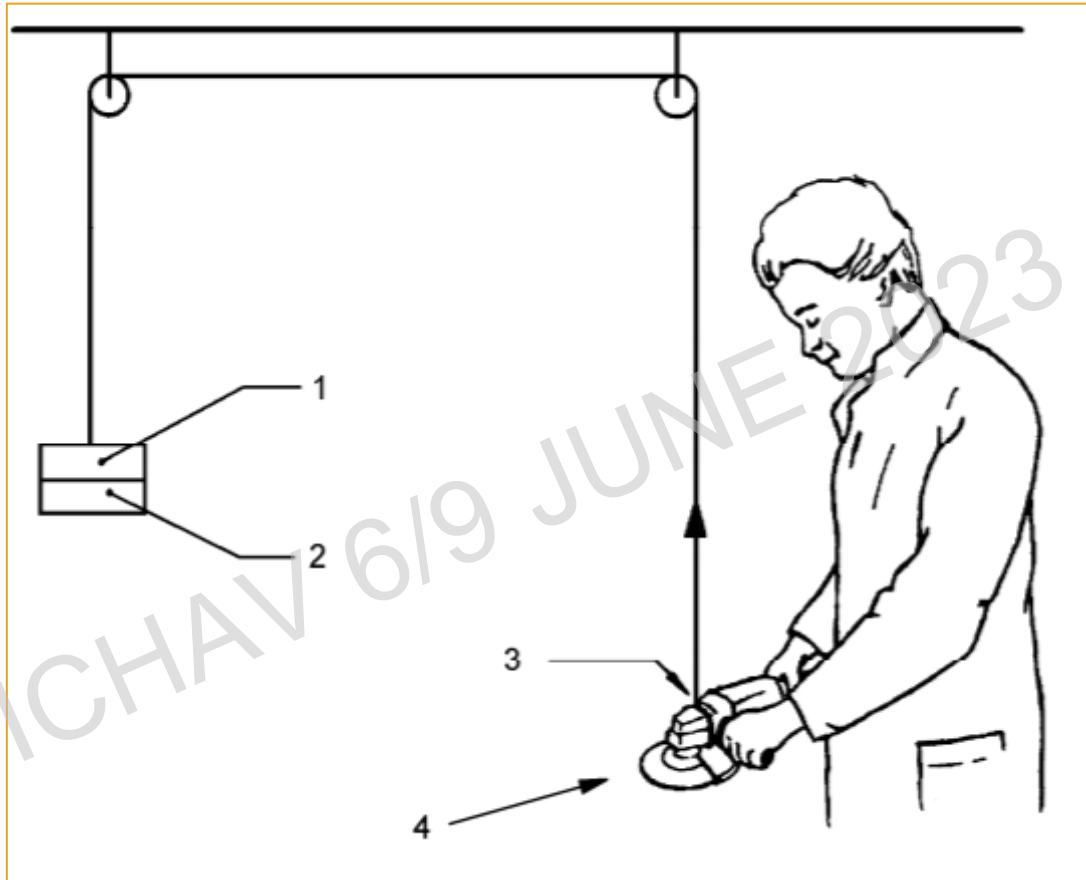
Standard EN 60745-2-3



To compare vibration emission of angle grinder  
➤ promote less vibrating machine

# First experimental tests: according to the standard EN 60745-2-3

## Standard EN 60745-2-3



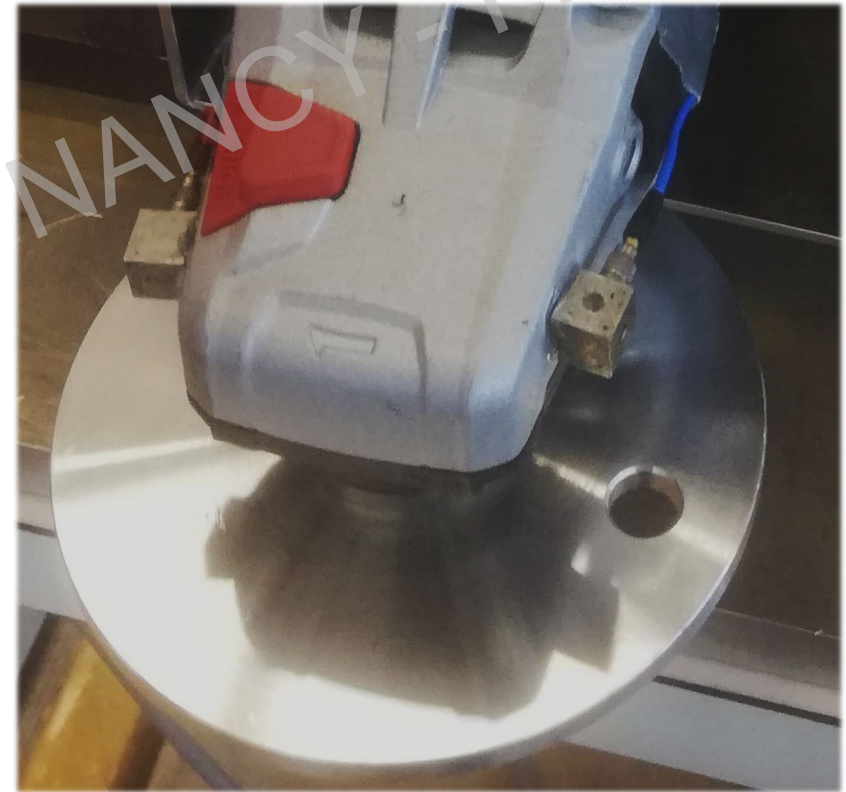
Standard disc with artificial unbalance

# First experimental tests: according to the standard EN 60745-2-3

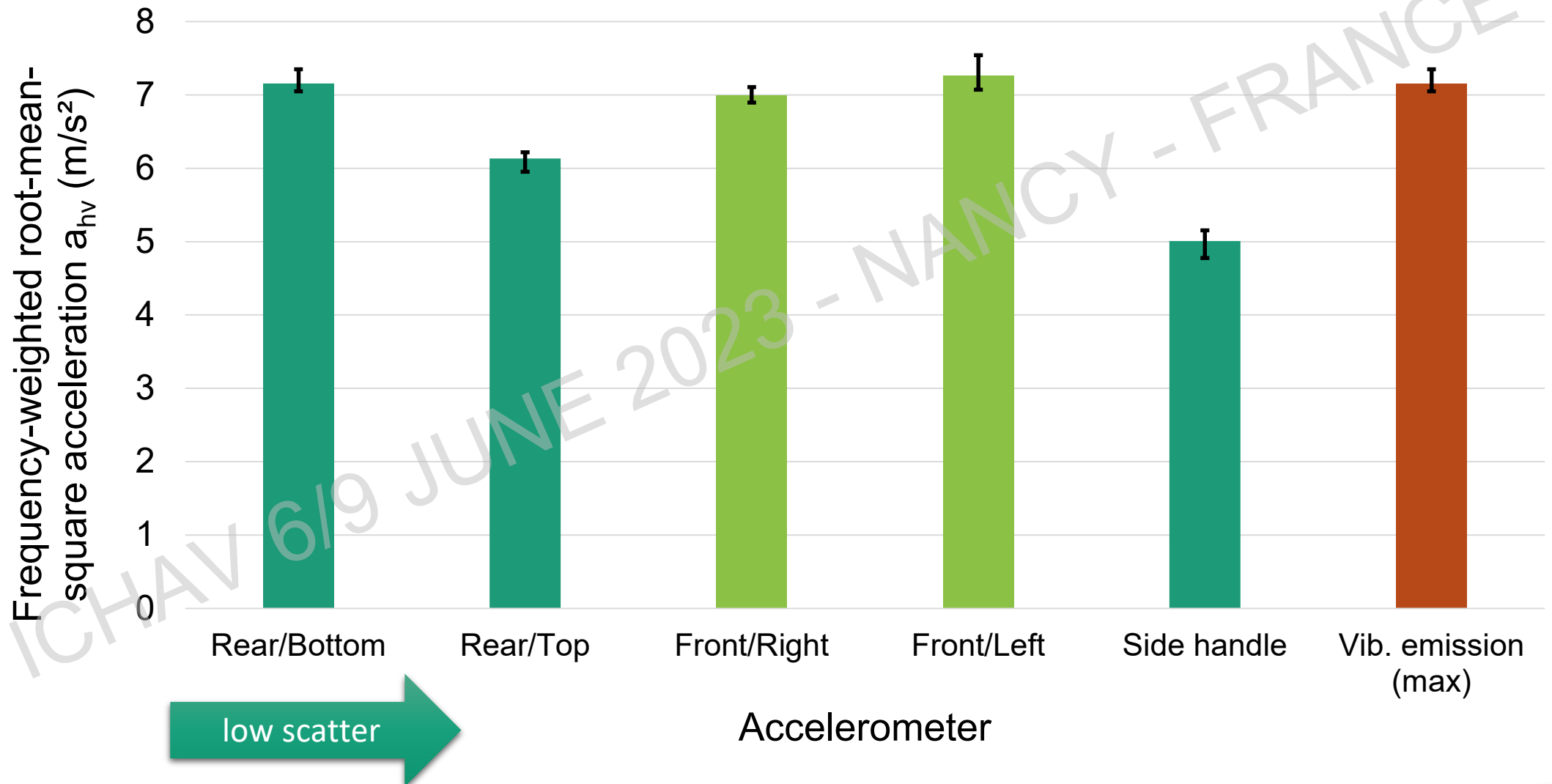
## Metabo W12-125 Quick



5 PCB triaxle piezoelectric accelerometers

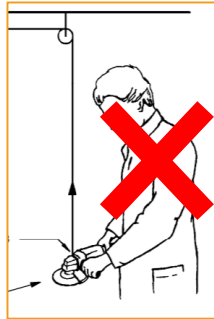


# First experimental tests: according to the standard EN 60745-2-3



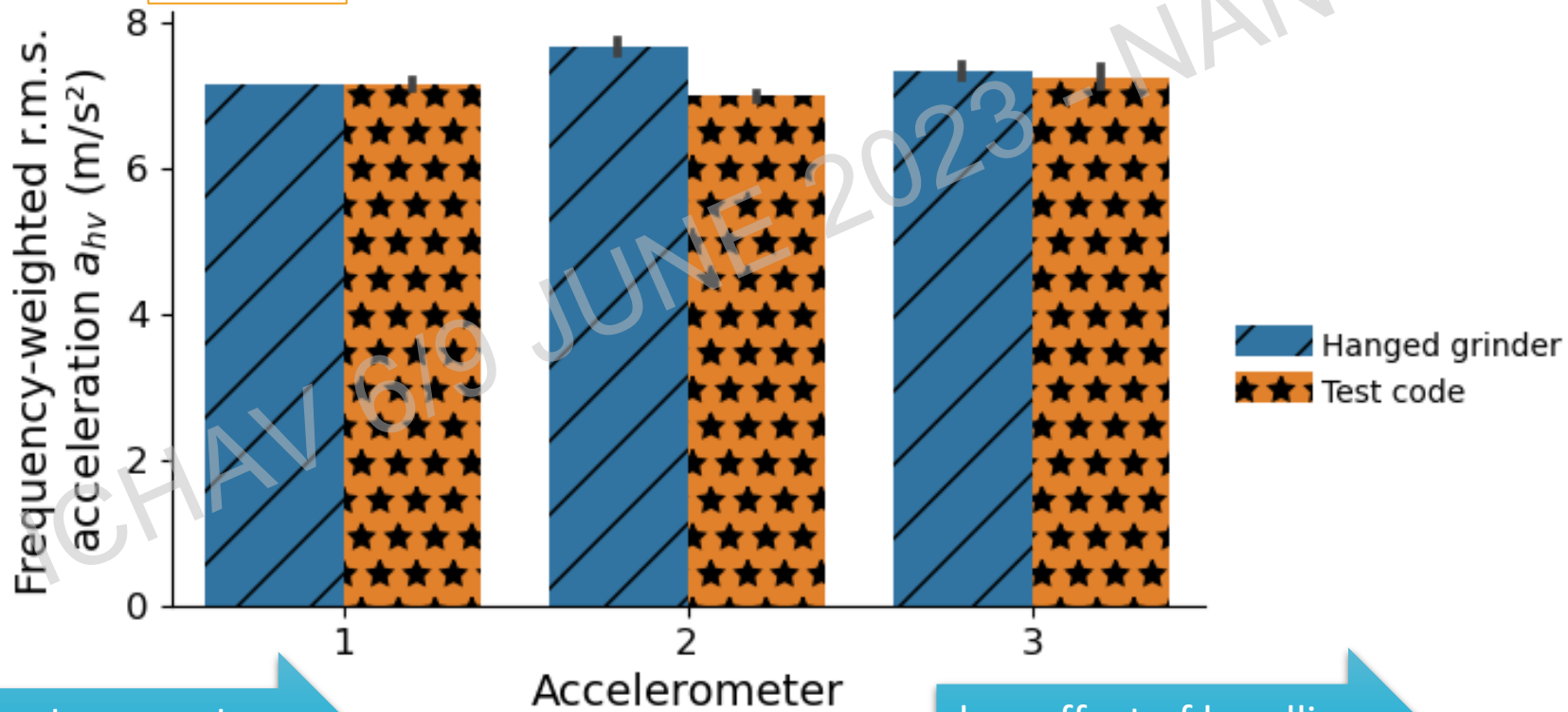
Note: error bars represents minimal and maximal values for 7 measurements

# Second experimental tests: hanged grinder



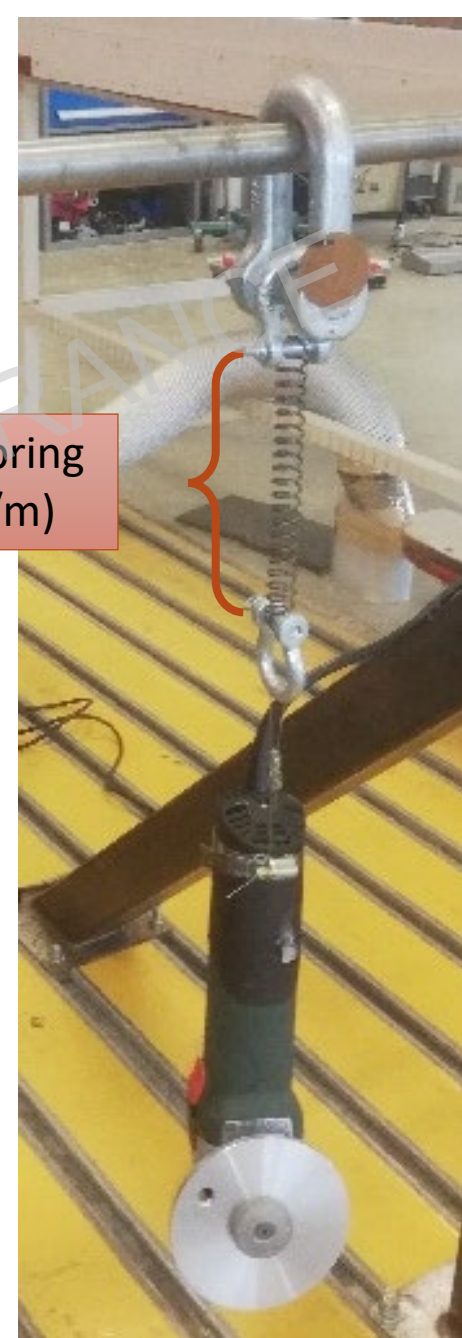
Second experimental tests: without operator and without side handle

Tension spring (1930 N/m)



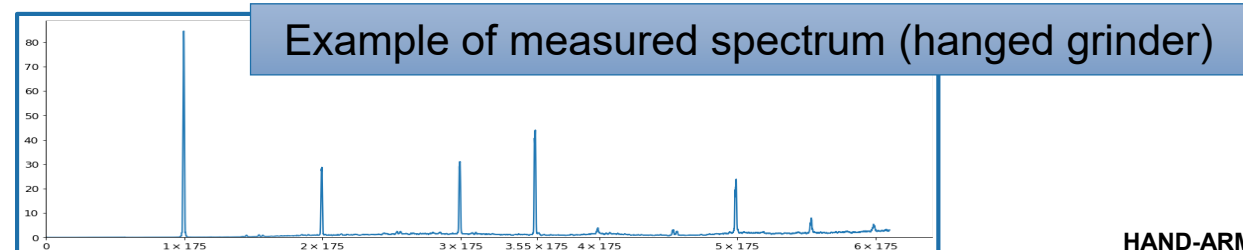
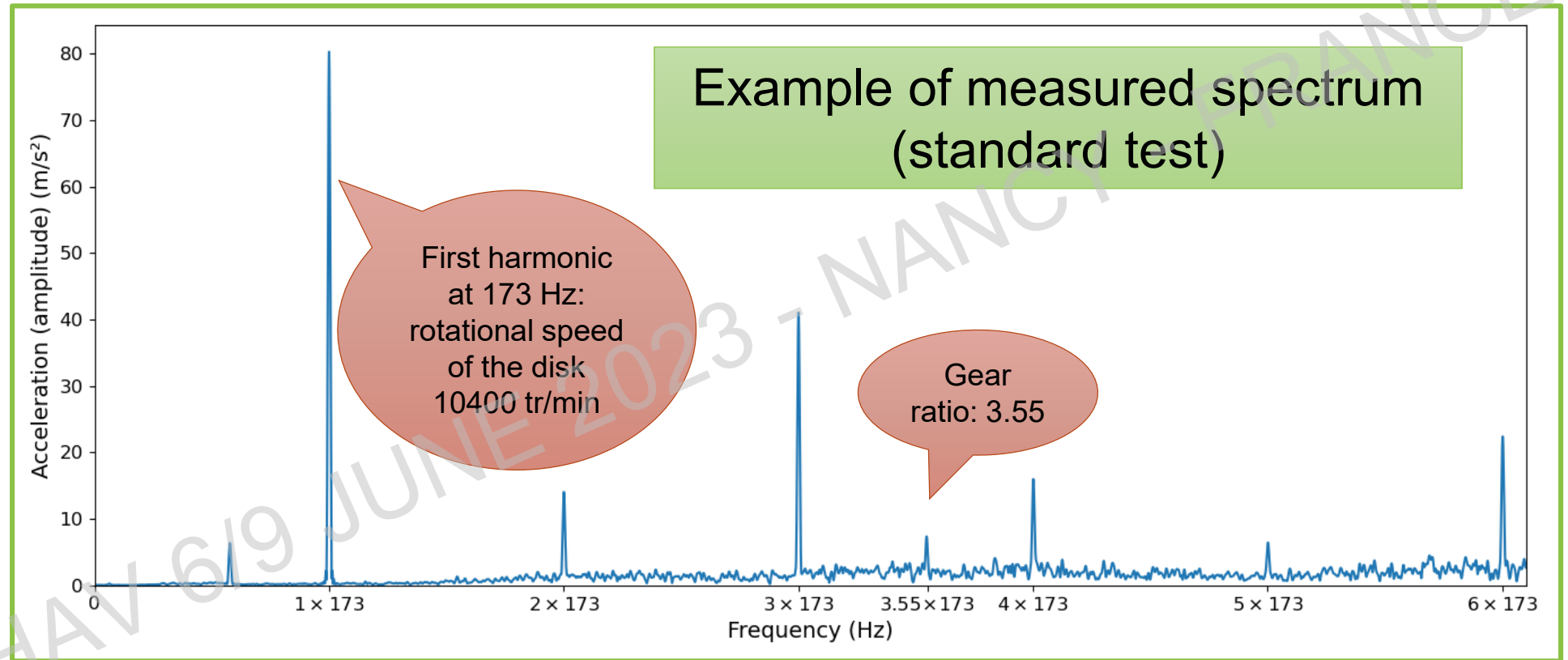
close results

low effect of handling

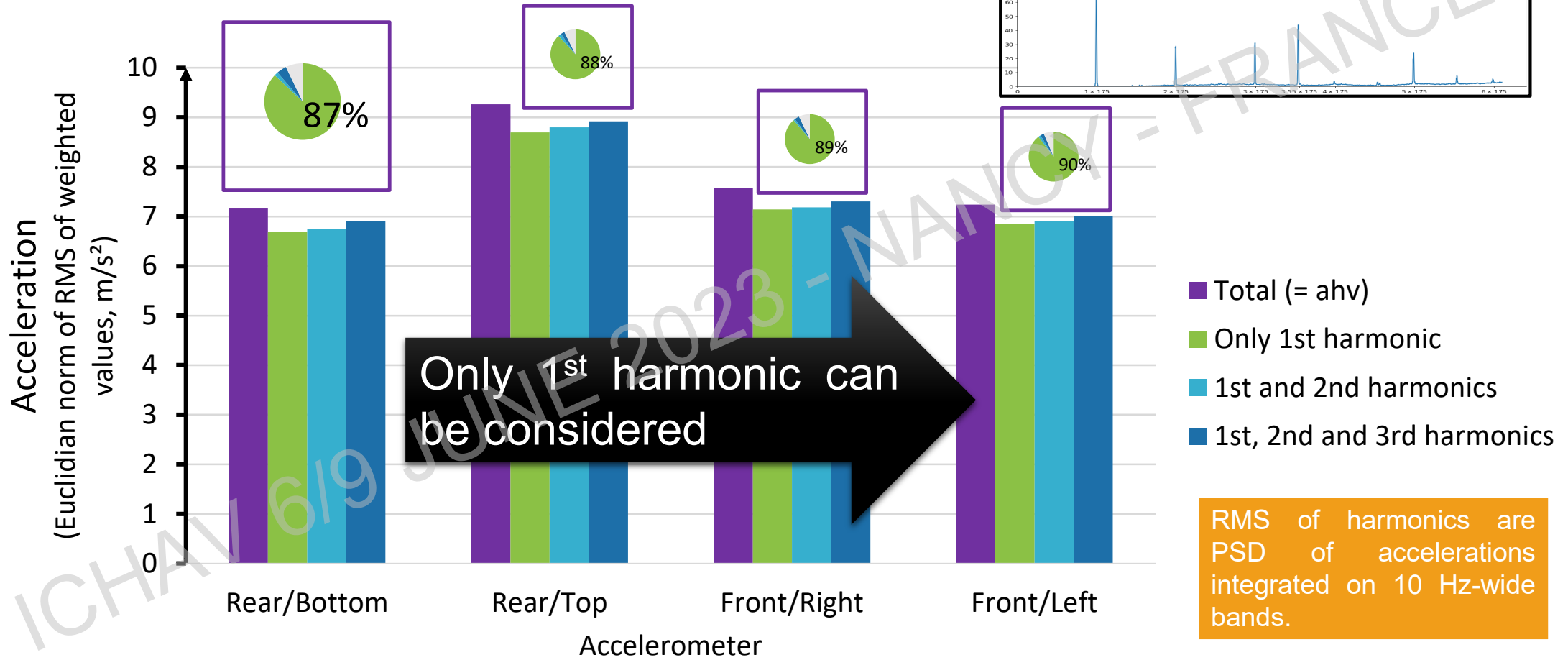




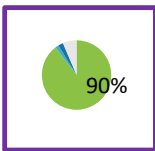
# Experimental tests: frequency analysis



# Second experimental tests: proportion of harmonics in RMS of weighted acceleration

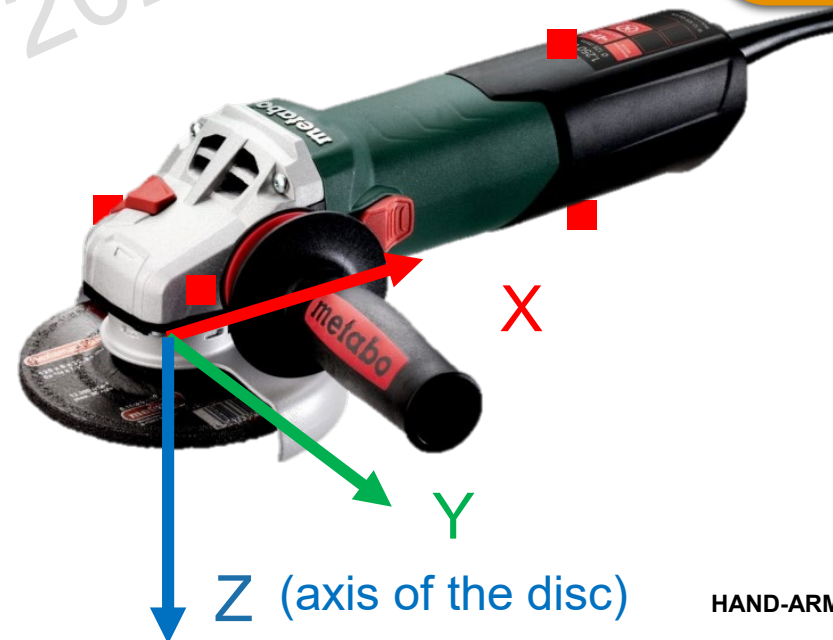
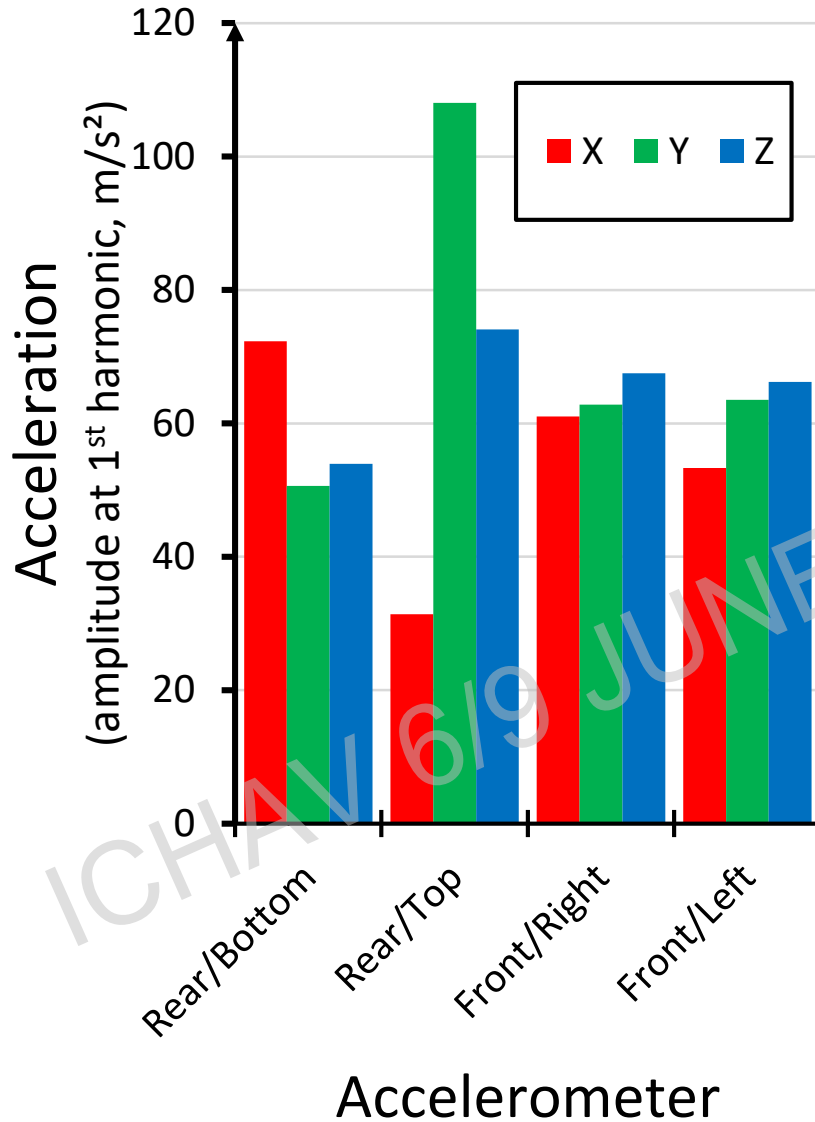


Only 1<sup>st</sup> harmonic can be considered



Proportion of mean squares of weighted acceleration  $\left(\frac{A_i^2}{a_{hv}^2}, (m/s^2)^2/(m/s^2)^2\right)$

# Second experimental tests: analysis of motion



# Second experimental tests: analysis of motion

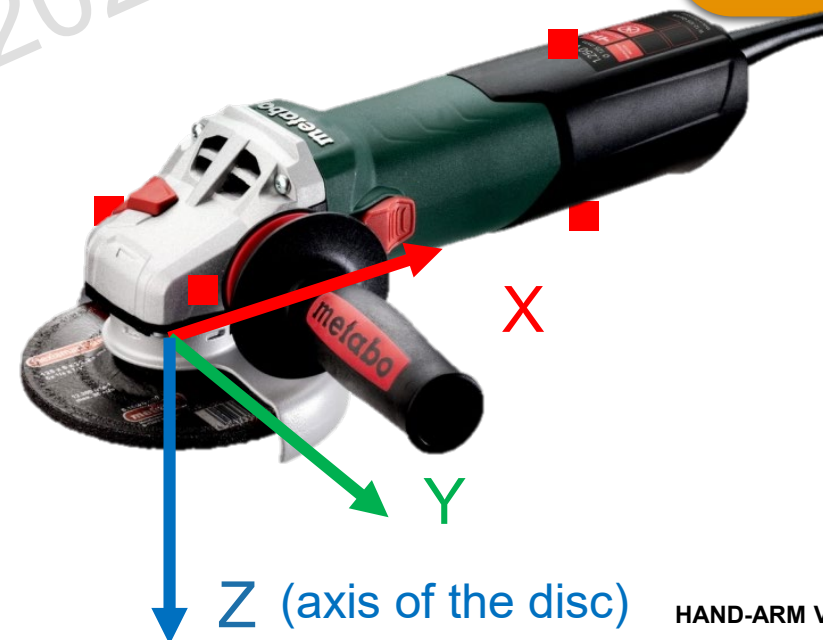
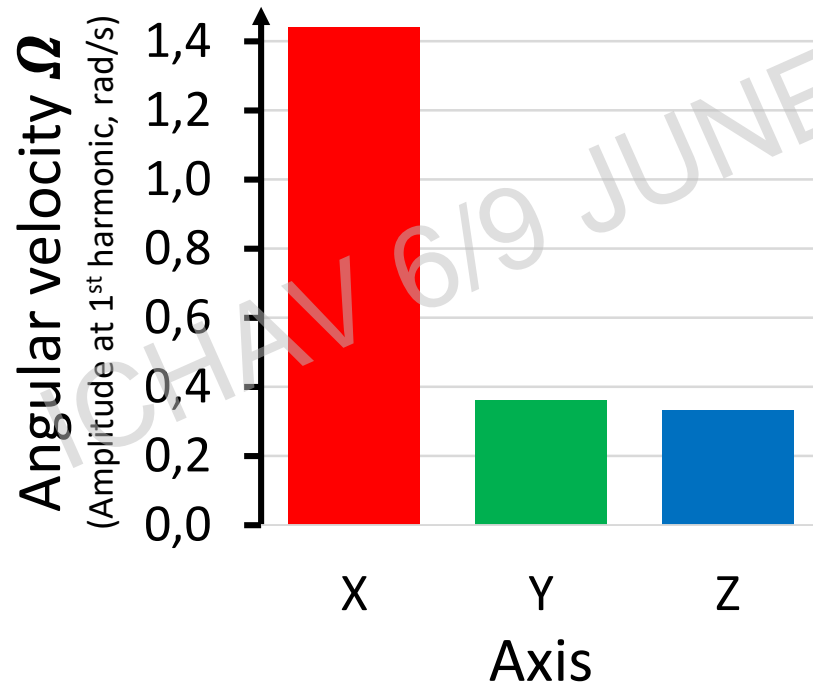
$\vec{\Omega}$  : Instantaneous angular velocity (rad/s)

According that :

$$\vec{v}_B - \vec{v}_A = \overrightarrow{BA} \wedge \vec{\Omega}$$

for a rigid body,

$\vec{\Omega}$  obtained by minimizing the matrix form of the previous formula with 4 complex amplitudes at 1<sup>st</sup> harmonic of velocities



Position and orientation of accelerometers on grinder measured by 3D scan

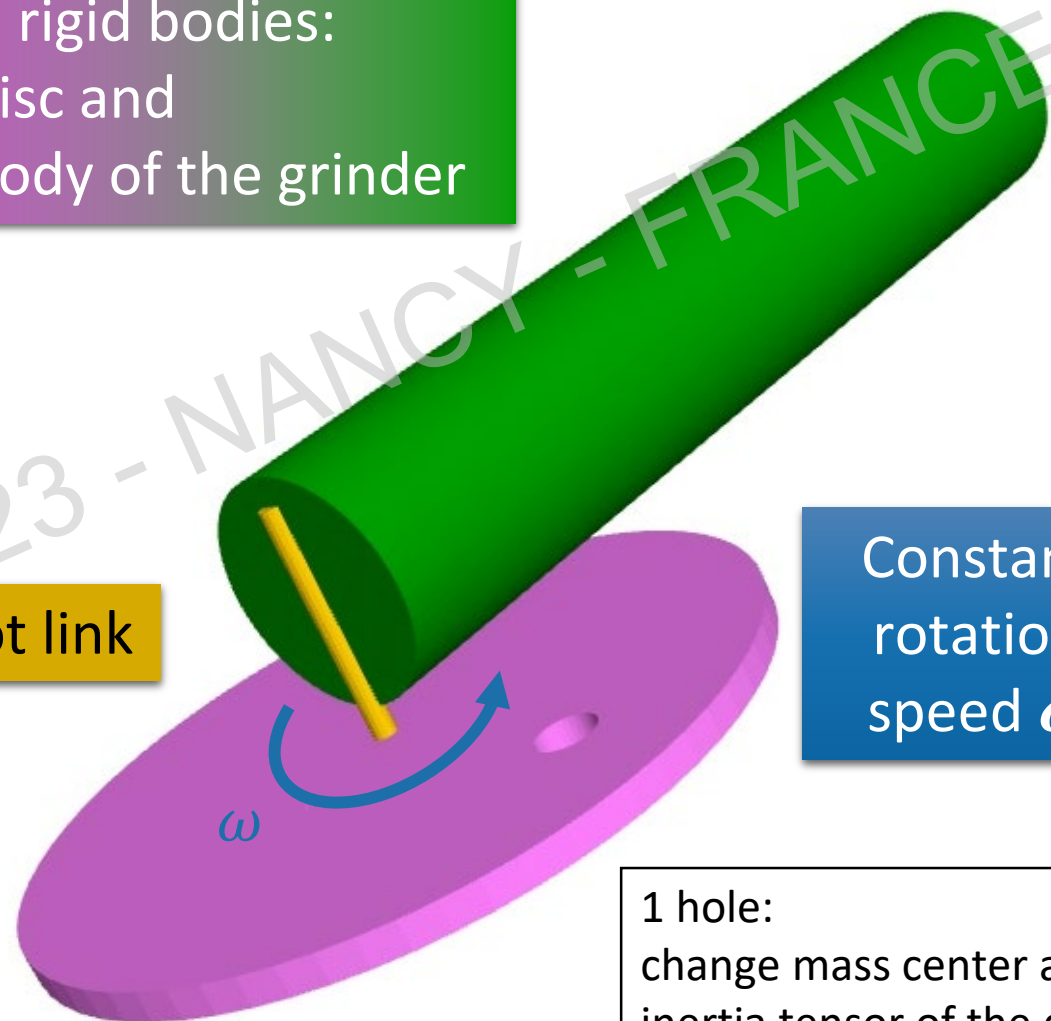


# Numerical Model



Two rigid bodies:  
1. disc and  
2. body of the grinder

1 pivot link



Constant rotation speed  $\omega$

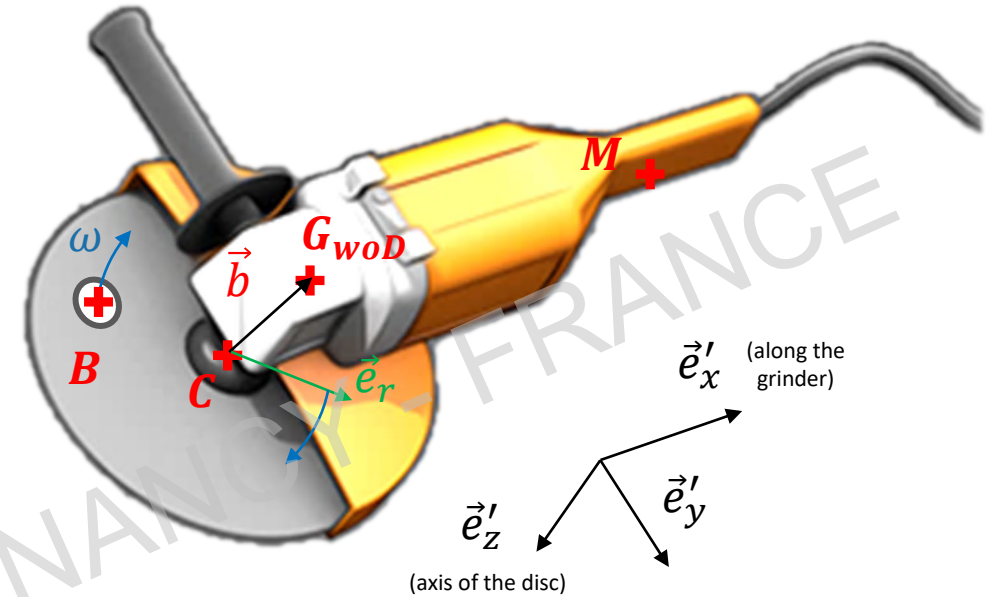
1 hole:  
change mass center and inertia tensor of the disc

Spring and gravity neglected:  
associated with low frequency modes,

$$\text{e.g.: } \frac{1}{2\pi} \sqrt{\frac{g}{L}} \approx 2 \text{ Hz}, \sqrt{\frac{k}{m}} \approx 30 \text{ Hz}$$

# Numerical Model

$M$	Point on the running grinder	$\vec{e}_r$	$-\vec{CB}/\ \vec{CB}\ $ , rotating vector in the plane of the disk
$C$	Center of the disk	bal	Imbalance of the perforated disk
$G_{woD}$	Center of mass of the grinder w/o the disk	$m_T$	Total mass of the system
$\vec{b} = \vec{CG}_{woD}$		$m_G$	Mass of the grinder w/o the disk
$\omega$	Rotational speed of the disk	$\bar{I}_T$	Sum of the inertia tensor of rigid bodies written in their center of mass
$\vec{\Omega}$	Angular velocity		



## Equations of motion of the grinder (steady-state, first harmonic, after simplifications)

( $\vec{a}_M$ ,  $\vec{\Omega}$  and  $\vec{e}_r$  represent complex amplitude at the frequency  $\omega/2\pi$ )

**Acceleration of a point M on the running grinder**

$$\vec{a}_M = \frac{\text{bal}}{m_T} \omega^2 \vec{e}_r + j\omega \vec{\Omega} \wedge \left( \vec{CM} - \frac{m_G}{m_T} \vec{b} \right)$$

**Angular velocity of the grinder**

$$\bar{I}_T \vec{\Omega} = j\omega m_G \frac{\text{bal}}{m_T} \vec{b} \wedge \vec{e}_r$$

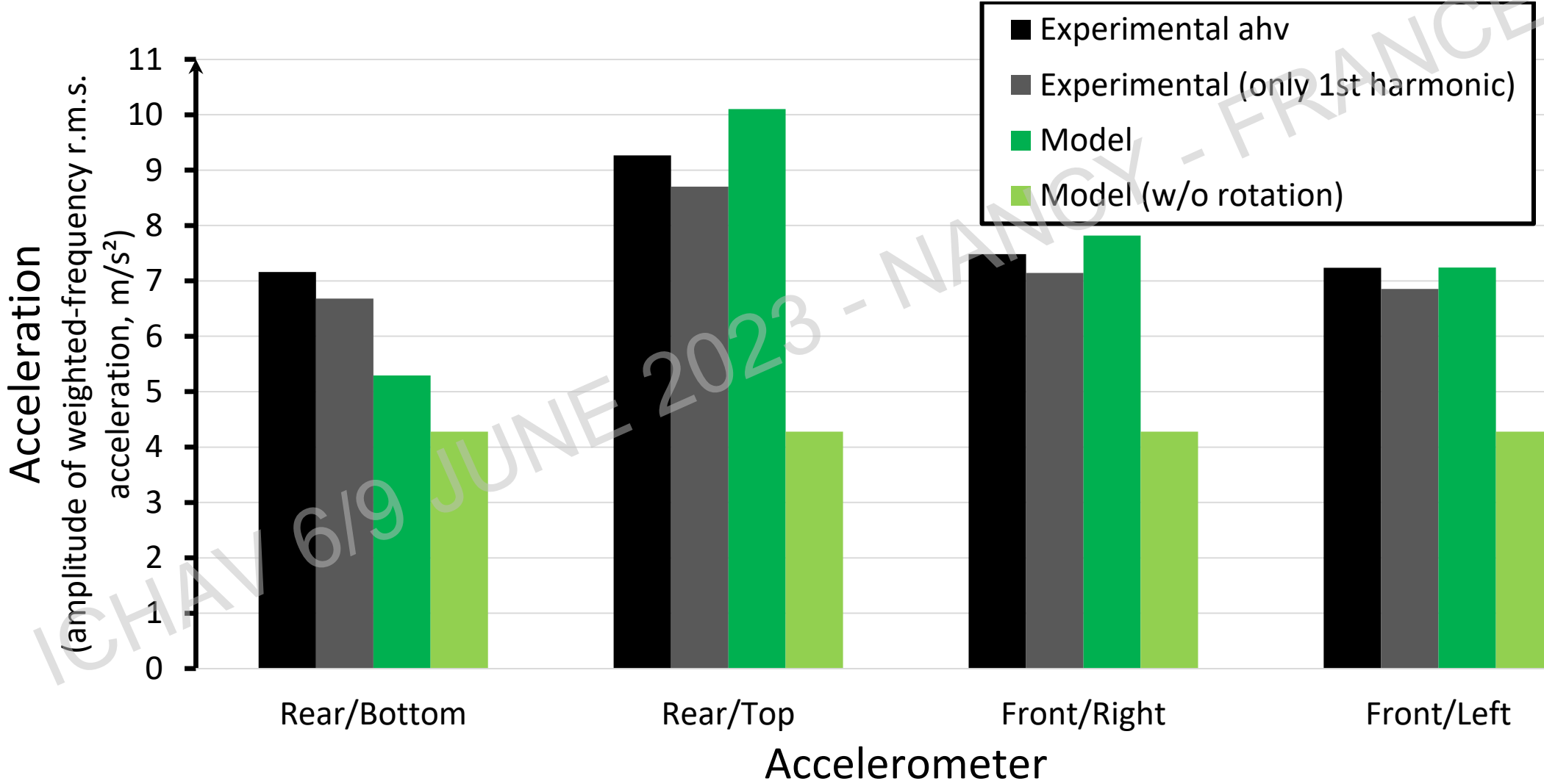
In the coordinate system linked to the grinder ( $\vec{e}'_x, \vec{e}'_y, \vec{e}'_z$ ), we can write:

$$\vec{e}_r \equiv \begin{pmatrix} 1 \\ i \\ 0 \end{pmatrix}, \vec{b} \equiv \begin{pmatrix} b_x \\ b_y \sim 0 \\ b_z \end{pmatrix}, \bar{I}_T \equiv \begin{pmatrix} I_{xx} & I_{xy} & I_{xz} \\ I_{xy} & I_{yy} & I_{yz} \\ I_{xz} & I_{yz} & I_{zz} \end{pmatrix}$$

and deduce  $\vec{\Omega}$  and  $\vec{a}_M$ .

# Numerical Model

Inertia moment tensor  $\bar{I}_B$  and center of mass  $G_{w0D}$ : provided by the manufacturer from their detailed CAD



# Discussion: second grinder with flexible handles

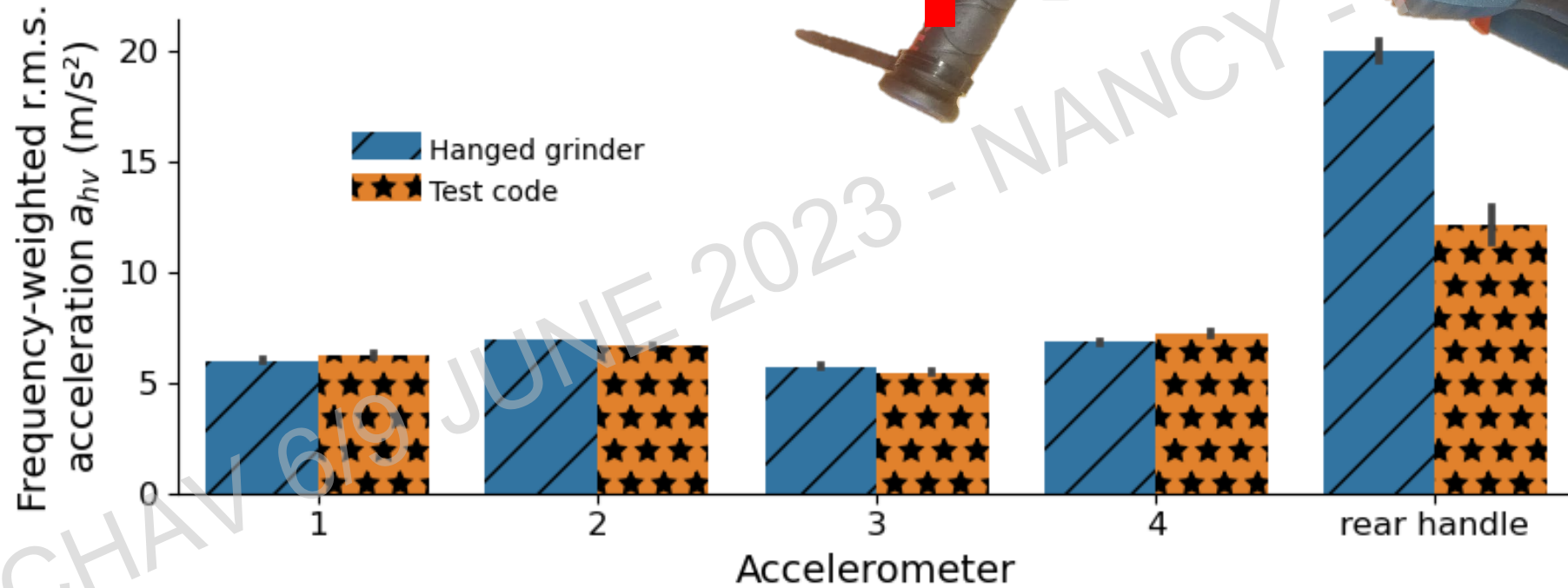


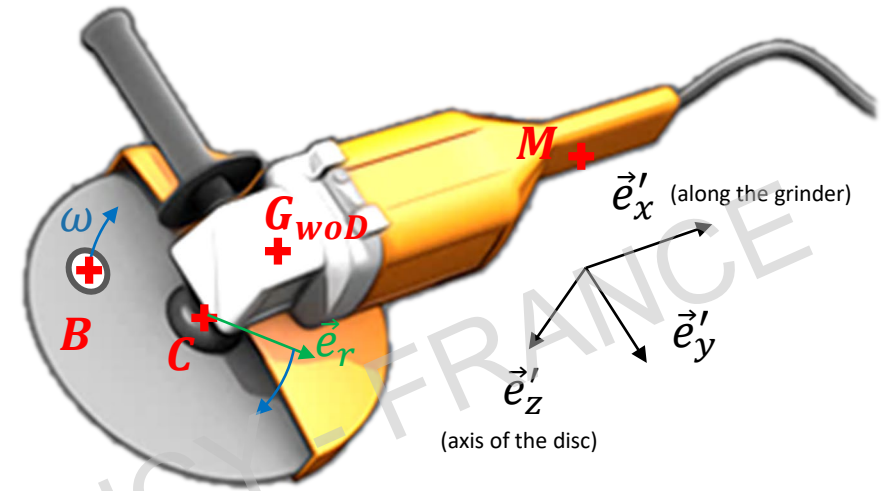
Figure 3: Frequency-weighted root-mean-square acceleration  $a_{hv}$  measured during test codes and tests with the hanging grinder. The vertical black lines indicate standard deviation.



# Discussion: ways to reduce vibration

Acceleration of a point M on the running grinder

$$\vec{a}_M \approx \omega^2 \frac{\text{bal}}{m_T} \left[ \vec{e}_r - \bar{\bar{I}}_T^{-1} (\overrightarrow{CG_{woD}} \wedge \vec{e}_r) \wedge \overrightarrow{G_{woD}M} \right]$$



1. reduce rotational speed of the disc  $\omega$ ,
2. increase mass of the grinder  $m_T$ ,
3. increase rotational inertia  $\bar{\bar{I}}_T$  by sharing mass far from mass center,
4. bring the center of mass  $G_{woD}$  closer to the hands or the center of disc  $C$
5. use flexible part  $\rightarrow$  model can be used to design flexible part

$M$	Point on the running grinder	$\vec{e}_r$	$-\overrightarrow{CB} / \ \overrightarrow{CB}\ $ , rotating vector in the plane of the disk
$C$	Center of the disk	bal	Imbalance of the perforated disk
$G_{woD}$	Center of mass of the grinder w/o the disk	$m_T$	Total mass of the system
$\omega$	Rotational speed of the disk	$\bar{\bar{I}}_T$	Sum of the inertia tensor of rigid bodies written in their center of mass